Suppose  $(X, \operatorname{dist}_X \text{ and } (Y, \operatorname{dist}_Y \text{ are metric spaces})$